

# ⇒ Thermodynamics

## 1) IDEAL GAS EQUATIONS-

$$PV = mRT$$

[abs]  $P = \text{Pascals}$   $R = \text{kJ/kgK}$

$V = \text{m}^3$

$m = \text{kg}$

$T = \text{K}$   
[abs]

$$pR = n\bar{R}$$

$n = \text{kmoles}$

$\bar{R} = 8.3140 \text{ kJ/kmole K}$

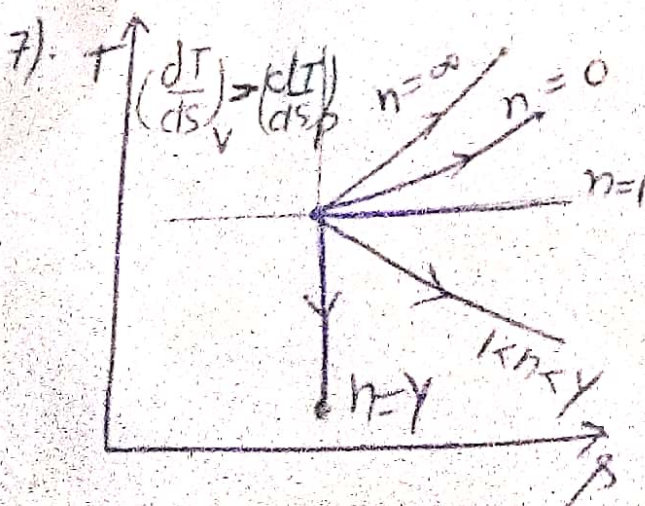
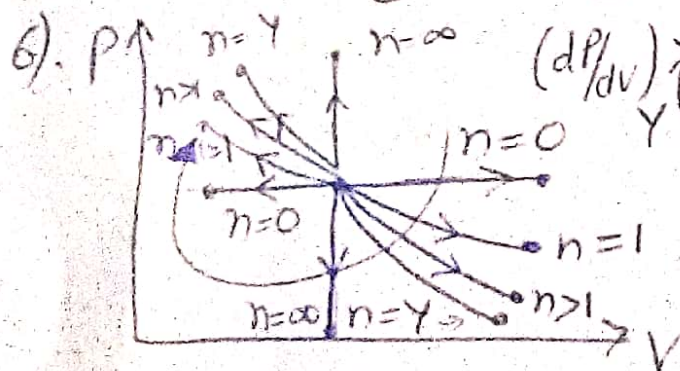
$$M = \frac{m}{n} \left( \frac{\text{kg}}{\text{kmole}} \right)$$

$$R = \frac{\bar{R}}{M}$$

3)  $0^\circ\text{C} = 273.15 \text{ K}$

4)  $P + f = C + 2$

$$\frac{^\circ\text{C}}{5} = \frac{^\circ\text{F} - 32}{9} = \frac{\text{K} - 273.15}{5}$$



## 3) First law of Thermodynamics

### a) for a Cycle:-

$$\oint dQ = \oint dW$$

IRReversible/  
Reversible

### b) for a process:-

$$dQ = dE + dW$$

for any system  
& Any process.

### c) कौनसा एव कौनसा लिखेंगे :-

$dQ = dE + dW \Rightarrow \text{Any process, Any Sys.}$

$dQ = dU + dW \Rightarrow \text{Any process, closed sys}$

$dQ = dU + PdV \Rightarrow \text{Reversible, closed sys}$

$dQ = Tds \Rightarrow \text{Reversible process.}$

$Tds = dU + PdV \Rightarrow \text{Rev / Irreversible (closed) both}$

$Tds = dH - VdP \Rightarrow \text{Rev / Irreversible (closed) both}$

### g) Raynighant eqn :-

$$\frac{T_2}{T_1} = \left( \frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}} = \left( \frac{V_1}{V_2} \right)^{\gamma-1}$$

for  $PV^\gamma = C$

$\frac{C_p}{C_v} = \frac{R}{\gamma-1} = 1.005 \text{ kJ/kgK}$

$C_p = \frac{R\gamma}{\gamma-1} = 0.718 \text{ kJ/kgK}$

$C_p - C_v = R = 0.287 \text{ kJ/kgK}$

$C_p/C_v = \gamma$



# 10). S.F.E.E°-

$$\dot{m}[h_1 + PE_1 + KE_1] + \dot{Q} = \dot{m}[h_2 + PE_2 + KE_2] + \dot{W}_{cv}$$

or

$$\dot{m}\left[h_1 + \frac{C_1^2}{2000} + \frac{gZ_1}{1000}\right] + \dot{Q} = \dot{m}\left[h_2 + \frac{C_2^2}{2000} + \frac{gZ_2}{1000}\right] + \dot{W}_{cv}$$

$$11). \left[ \text{COP} \right]_{H.P} = \left[ \text{COP} \right]_{\text{Ref}} + 1 = \frac{1}{\eta_{H.E}}$$

Cond<sup>n</sup>:- Working all B/w Same Temp<sup>r</sup> limits

## 12). Clausius Inequality:-

$$\oint \frac{dQ}{T} \leq 0 \quad \oint \frac{dQ}{T} < \text{Irrevers.} \\ = \text{Rev.} \\ > \text{Impossible.}$$

## 13). Third Law of thermodynamics

$$\Delta S_{\text{univ}} \geq 0$$

## 14). (Law of degradation of energy). Second law of thermodynamics

$$W = HGE \quad \& \quad Q = LGE$$

W  $\xrightarrow{\text{fully}} \rightarrow$  Q  
(converts)

But Reverse is not possible or Mathematically:-

$$\eta_{H.E} < 100\%$$

$$15). [1 - \eta_{\text{comb}}] = [1 - \eta_I][1 - \eta_{II}]$$

## 15). Entropy change of a system:-

$$a). \int_1^2 ds = C_v \ln \left[ \frac{T_2}{T_1} \right] + R \ln \left[ \frac{V_2}{V_1} \right]$$

$$b). \int_1^2 ds = C_p \ln \left[ \frac{T_2}{T_1} \right] - R \ln \left[ \frac{P_2}{P_1} \right]$$

$$c). \int_1^2 ds = C_p \ln \left[ \frac{V_2}{V_1} \right] + C_v \ln \left[ \frac{P_2}{P_1} \right]$$

## 16). Slopes:- of T-s curve.

$$\left( \frac{dT}{ds} \right)_p = \frac{T}{C_p}, \quad \left( \frac{dT}{ds} \right)_v = \frac{T}{C_v}$$

$$\left( \frac{dU}{dT} \right)_p = C_p, \quad \left( \frac{dU}{dT} \right)_v = C_v$$

$\left( \frac{dh}{ds} \right)_p = T$  (Mollier chart)

## 17). Availability & Irreversibility

A.E = Maximum Amount of Work

$$A.E = Q_1 - T_0 \Delta S \rightarrow U.A.E$$

$$\text{Loss of A.E} = \uparrow \text{in U.A.E} = Q_{T_0} \left[ \frac{T_2 - T_1}{T_1 T_2} \right]$$

[Irreversibility]

[Closed System:-]

$$W_{\text{max}} = [U_i - U_f] - T_0 [S_i - S_f]$$

$$W_{\text{max obtainable work}} = [U_i - U_f] - T_0 [S_i - S_f] - P_0 \Delta V$$

## Gibbs Helmholtz f<sup>n</sup>:- (Used)

$$F = U - TS$$



## OPEN SYSTEM -

$$W_{\max} = W_{\max \text{ obtainable work}}$$

$$= [H_i^o - H_f] - T_o [S_i^o - S_f]$$

Gibbs f<sup>n</sup> -

$$G = H - TS$$

18. -

φ [Availability f<sup>n</sup>s] -

Closed

open

$$\phi_c = U - TS - P_o V$$

$$\phi_o = H - T_o S$$

$$W_{\max \text{ obt. work}} = \phi_1 - \phi_2$$

19). Second Law Efficiency:-

$$\eta_{\text{Second law}} = \frac{\eta_{\text{Actual}}}{\eta_{\text{ideal}}} = \frac{\eta_{\text{Actual cycle}}}{\eta_{\text{Carnot cycle}}}$$

20). Vander-waals Eq<sup>n</sup> -

$$\left[ P + \frac{a}{V^2} \right] [V - b] = RT$$

21). Mixing:-

$$C_{\text{mix}} = \frac{m_1 C_1 + m_2 C_2 + m_3 C_3 + \dots}{m_1 + m_2 + m_3 + \dots}$$

$$h_{\text{mix}} = \frac{m_1 h_1 + m_2 h_2 + \dots}{m_1 + m_2 + \dots}$$

$$R_{\text{mix}} = \frac{m_1 R_1 + m_2 R_2 + \dots}{m_1 + m_2 + \dots}$$

$$x_i = \frac{n_i}{n_1 + n_2} \text{ fraction.}$$

$$P_i = x_i P_{\text{mix}}$$

Solid  $\xrightarrow[\text{Sublimation}]{\text{Directly}}$  Vapour

22). THERMODYNAMIC RELATIONS -

$$Tds = du + PdV \rightarrow 1^{\text{st}} T-ds \text{ eq<sup>n</sup>}$$

$$Tds = dh - vdp \rightarrow 2^{\text{nd}} T-ds \text{ eq<sup>n</sup>}$$

$$Tds = C_v dT + T \left( \frac{\partial P}{\partial T} \right)_V dV$$

$$Tds = C_p dT - T \left( \frac{\partial V}{\partial T} \right)_P dP$$

$$du = C_v dT + \left[ T \left( \frac{\partial P}{\partial T} \right)_V - P \right] dV$$

$$dh = C_p dT - \left[ T \left( \frac{\partial V}{\partial T} \right)_P - V \right] dP$$

$$C_p - C_v = -T \left[ \frac{\partial V}{\partial T} \right]_P^2 \left( \frac{\partial P}{\partial V} \right)_T = \frac{T V \beta^2}{\kappa_T}$$

$$\beta = \text{Volume expansivity} = \frac{1}{V} \left( \frac{\partial V}{\partial T} \right)_P$$

$$\kappa_T = \text{Isothermal compress.} = \frac{1}{P} \left( \frac{\partial P}{\partial V} \right)_T = -\frac{1}{V} \left( \frac{\partial V}{\partial P} \right)_T$$

$$\alpha_j^o = \left( \frac{dT}{dP} \right)_f = \frac{1}{C_p} \left[ T \left( \frac{\partial V}{\partial T} \right)_P - V \right]$$

$$\alpha_j^o = 0 \text{ for Ideal gas.}$$

$$\left( \frac{dP}{dT} \right)_{\text{sat. v}} = \frac{S_g - S_f}{V_g - V_f} = \frac{h_{fg}}{T(V_g - V_f)} = \frac{P(L.H)}{T^2 R}$$

Maxwell's Relations -

$$1) \left( \frac{\partial T}{\partial V} \right)_S = - \left( \frac{\partial P}{\partial S} \right)_V$$

$$2) \left( \frac{\partial T}{\partial P} \right)_S = \left( \frac{\partial V}{\partial S} \right)_P$$

$$3) \left( \frac{\partial P}{\partial T} \right)_V = \left( \frac{\partial S}{\partial V} \right)_T$$

$$4) \left( \frac{\partial V}{\partial T} \right)_P = - \left( \frac{\partial S}{\partial P} \right)_T$$



## 23) THERMODYNAMICS के बीच

## सुख CONCEPTS:-

Value of  $n$ :-

$n = 1.6666$  for Monatomic

$n = 1.4$  for air (diatomic)

$n = 1.3333$  for polyatomic.

## 24) CONTROL VOLUME WORK

[OPEN SYS. WORK]  $[W_{c.v}]$

S.F.E.E [APE = ΔKE = 0]

If  $Q$  = known

If  $Q$  = unknown

$$Q_{in} + Q = h_e + W_{c.v}$$

$$W_{c.v} = \int_i^e -V dp$$

## 25) $Q, U, H, S$ [Heat, I.E, ENTHALPY & ENTROPY]:-

$Q \Rightarrow$  [Heat]:- Always valid

$$Q_v = dU$$

$$Q_p = dH$$

$U$ :- Internal Energy:-

$Q = C_v$  for Solids & Liquid's

Liquid's & Solids:-

$$dU = m C_{p/v} dT$$

Ideal gas:-

$$dU = m C_v dT$$

H [Enthalpy]:-  $h = u + P v$

a) Solid & liquids:- [ $V = \text{const.}$ ]

$$dh = du + P dv + v dp$$

$$dh = C dT + v dp$$

b) Ideal gas  $\Rightarrow C = C_p$

$$dh = C_p dT$$

S [Entropy]:-

a) Solid & liquids:- ( $V = C$ )

$$S_2 - S_1 = m [C_p = C_v] \ln [T_2/T_1] + R \ln [V_2/V_1] \rightarrow 0$$

b) Ideal gas:-

$$S_2 - S_1 = C_p \ln [T_2/T_1] - R \ln [P_2/P_1] = C_v \ln (T_2/T_1) + R \ln (V_2/V_1)$$

c) Reservoir or phase change:-

$$[T = \text{const.}] \quad S_2 - S_1 = \int \frac{dQ}{T} = \frac{Q}{T}$$

Atmospheric pressure conditions

$$1 \text{ atm} = 1.01325 \text{ bar} = 10.3 \text{ m of water column}$$

26) Triple point [WATER]

$$T_{tr} = 0.01^\circ\text{C} = 273.16 \text{ K}$$

$$P_{tr} = 611.97 \text{ N/m}^2$$

27) Critical point [WATER]

$$T_c = 374^\circ\text{C}$$

$$P_c = 221.2 \text{ bar}$$

$$V_c = 0.003175 \text{ m}^3/\text{kg}$$



# THERMODYNAMICS

1)  $\frac{dU_{cv}}{dt} = [\dot{m}_i \cdot h_i + \dot{Q}] - [\dot{m}_e \cdot h_e + \dot{W}]$

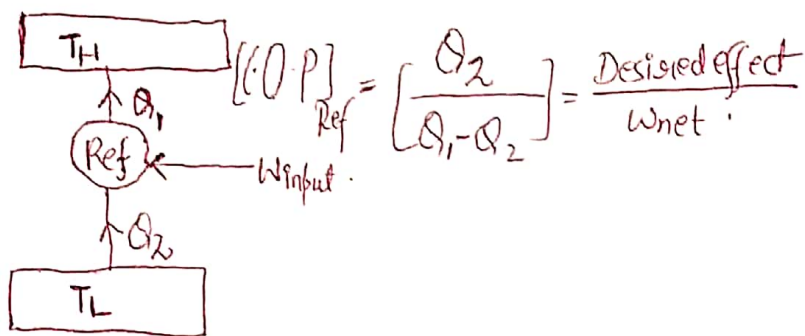
2)  $\frac{dm_{cv}}{dt} = \dot{m}_i - \dot{m}_e = \dot{m}_1 - \dot{m}_2$

$\gamma = 1.66667$  for Monatomic gas

$\gamma = 1.40$  for Diatomic gas /  $\gamma_{air} = 1.40$

$\gamma = 1.33$  for Polyatomic

3).



4) Heat Added / Rejected at const. pressure ( $P=c$ ) :- [In Pure Substance]  
then us. -

$$dQ = dh - \cancel{v dp} \rightarrow 0$$

$$[Q_{1-2}] = [h_2 - h_1] \text{ kJ/kg.}$$

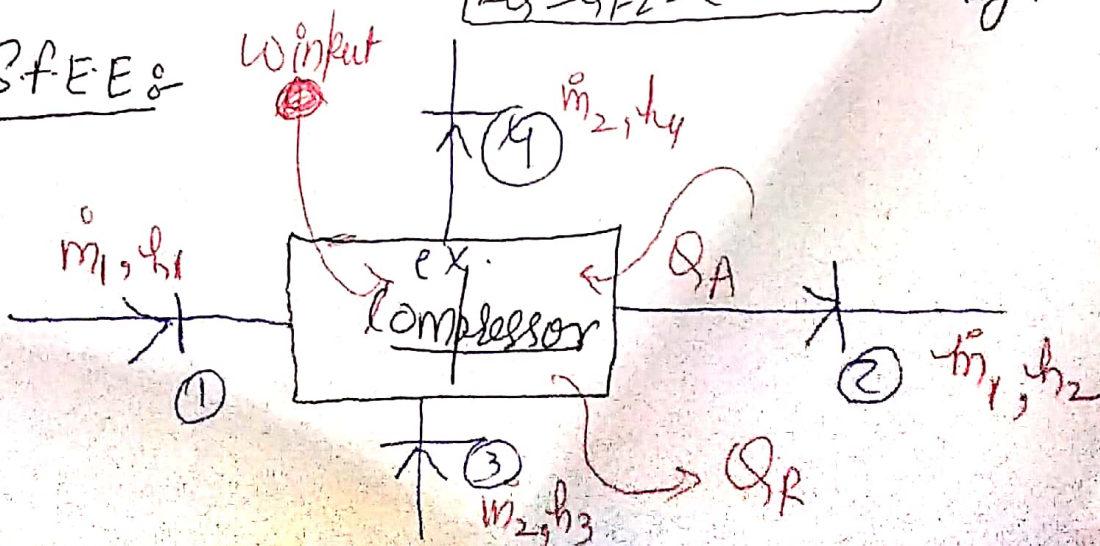
5) Heat Added / Rejected at const. Volume ( $V=c$ ) :- [In pure Substance]

$$dQ = dU + \cancel{P dv} \rightarrow 0$$

$$(dQ) = (dU)$$

$$[Q_{1-2} = (U_2 - U_1)] \text{ kJ/kg.}$$

6) S.F.E.E &



$$\Delta S = \bar{R} n_1 \ln \left( \frac{u_1}{u_2} \right) + n_2 \bar{R} \ln \left( \frac{u_2}{u_1} \right)$$


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$$x = \frac{u_1}{u_1 + u_2}$$

$$E_{\text{inter}} = E_{\text{outlet}}$$